

Name: _____

Date: _____

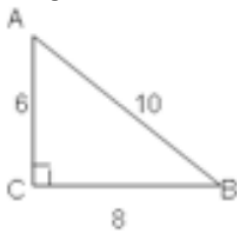
UNIT 6

LESSON 8

AIM: WHAT ARE COFUNCTIONS?

Do Now: If two **complementary** angles are represented by $4x$ and $7x - 9$, what is the value of x ?

Determine the following:



$\sin A =$

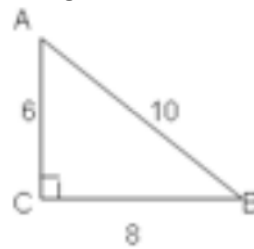
$\cos B =$

What is the *measure* of angle A?

What is the *measure* of angle B?

What is the relationship between these angles?

Determine the following:



$\sin B =$

$\cos A =$

What is the *measure* of angle A?

What is the *measure* of angle B?

What is the relationship between these angles?

SINE AND COSINE OF COMPLEMENTARY ANGLES

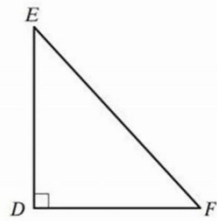
If A and B are complementary angles,

$$\boxed{\begin{array}{l} \sin A = \cos B \\ \cos A = \sin B \end{array}}$$

When $0^\circ < \theta < 90^\circ$, $\sin(90^\circ - \theta) = \cos \theta$ and $\sin \theta = \cos(90^\circ - \theta)$

Therefore, sine and cosine are called _____ !

1. In right triangle DEF, where $m\angle D = 90^\circ$, which of the following statements is always true?



- 1) $\sin D = \cos F$
- 2) $\tan E = \cos F$
- 3) $\sin F = \cos E$
- 4) $\tan D = \sin E$

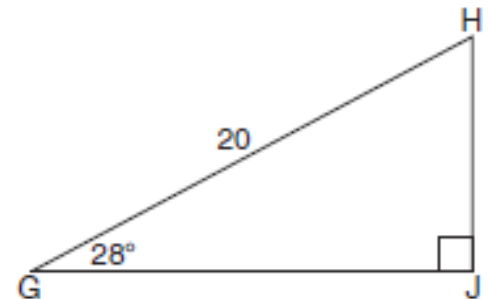
2. In right triangle ABC, where $m\angle B = 90^\circ$, which of the following statements is always true?

- 1) $\sin A = \cos B$
- 2) $\sin A = \cos C$
- 3) $\tan A = \cos C$
- 4) $\sin A = \tan B$

3. Each of the following diagrams and examples is a right triangle. Fill in the blanks based on the sine & cosine of angles that add to 90°

	Right Triangle ABC with $m\angle C = 90^\circ$.	Right Triangle DEF with $m\angle E = 90^\circ$.	
$\sin \underline{\hspace{1cm}} = \cos \underline{\hspace{1cm}}$ or $\sin \underline{\hspace{1cm}} = \cos \underline{\hspace{1cm}}$	$\sin \underline{\hspace{1cm}} = \cos \underline{\hspace{1cm}}$ or $\sin \underline{\hspace{1cm}} = \cos \underline{\hspace{1cm}}$	$\sin \underline{\hspace{1cm}} = \cos \underline{\hspace{1cm}}$ or $\sin \underline{\hspace{1cm}} = \cos \underline{\hspace{1cm}}$	$\sin \underline{\hspace{1cm}} = \cos \underline{\hspace{1cm}}$ or $\sin \underline{\hspace{1cm}} = \cos \underline{\hspace{1cm}}$

4. When instructed to find the length of \overline{HJ} in right triangle HJG , Jia wrote the equation $\sin 62^\circ = \frac{GJ}{20}$ while Dan wrote $\cos 28^\circ = \frac{GJ}{20}$. Are both students' equations correct? Explain why.



Sine & Cosine of Angles that add to 90°

$\sin A = \cos B$ if $A + B = \underline{\hspace{1cm}}^\circ$

5. Solve the following.

a) $\sin 27^\circ = \cos \underline{\hspace{1cm}}^\circ$

b) $\cos 55^\circ = \sin \underline{\hspace{1cm}}^\circ$

c) $\sin 17.8^\circ = \cos \underline{\hspace{1cm}}^\circ$

d) $\cos 90^\circ = \sin \underline{\hspace{1cm}}^\circ$

e) $\cos 45^\circ = \sin \underline{\hspace{1cm}}^\circ$

f) $\sin 62\frac{2}{3}^\circ = \cos \underline{\hspace{1cm}}^\circ$

6. Find the value of θ that will make the equation $\sin \theta = \cos 37^\circ$ true when $0^\circ < \theta < 90^\circ$. Explain your answer.

7. In a right triangle, $\sin(2x-15)^\circ = \cos(x-12)^\circ$. What is the value of x ?

8. In a right triangle, $\sin(x+5)^\circ = \cos(4x+10)^\circ$. What is the value of x ?

9. Find the value of B that will make the equation $\sin 62^\circ = \cos B$ true when $0^\circ < B < 90^\circ$. Explain your answer.

NOW YOU TRY SOME! For questions 1-6, find values for θ that make each statement true:

1. $\sin\theta = \cos 25^\circ$

2. $\sin 80^\circ = \cos\theta$

3. $\sin\theta = \cos(\theta + 10)^\circ$

4. $\sin(\theta - 45)^\circ = \cos\theta$

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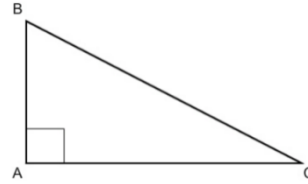
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UNIT 6

LESSON 8

HOMEWORK

1. In scalene triangle ABC shown in the diagram below, $m\angle A = 90^\circ$. Which equation is always true?



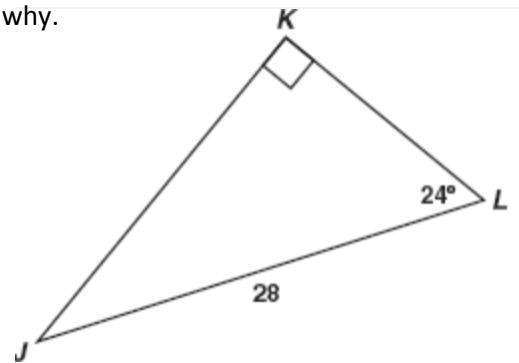
- 1) $\cos C = \cos B$
- 2) $\sin C = \sin B$
- 3) $\sin B = \cos C$
- 4) $\cos B = \sin A$

2. In a right triangle, $\sin(5x + 15)^\circ = \cos(4x - 6)^\circ$. What is the value of x ?

4. Find the value of B that will make the equation $\sin 89^\circ = \cos B$ true when $0^\circ < B < 90^\circ$. Explain your answer.

3. When instructed to find the length of \overline{KL} in right triangle HJG , Conor wrote the equation $\cos 24^\circ = \frac{KL}{28}$ while

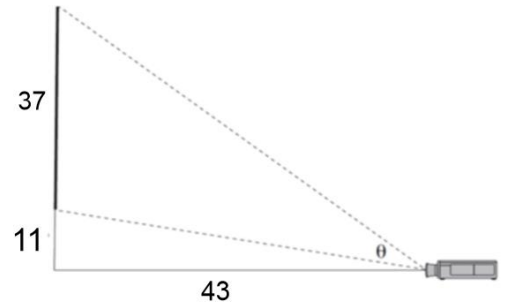
Steve wrote $\sin 66^\circ = \frac{KL}{28}$. Are both students' equations correct? Explain why.



Review Question

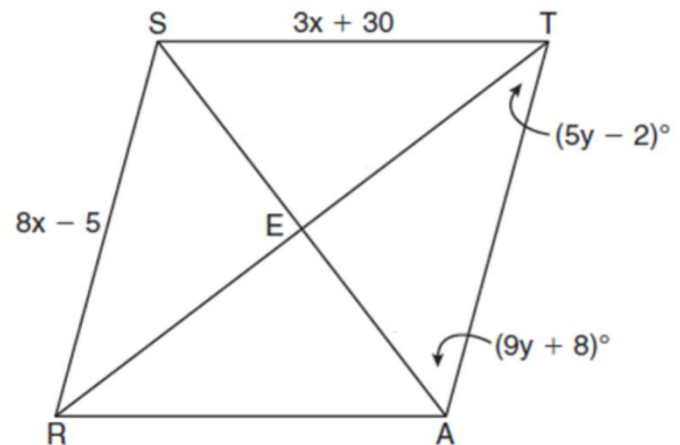
5. As modeled below, a movie is projected onto a large outdoor screen. The bottom of the 37-foot-tall screen is 11 feet off the ground. The projector sits on the ground at a horizontal distance of 43 feet from the screen. Determine and state, to the *nearest tenth of a degree*, the measure of θ , the projection angle.

(Hint: Find the big angle of elevation, small angle of elevation and subtract!)



6. In the diagram below, quadrilateral $STAR$ is a **rhombus** with diagonals \overline{SA} and \overline{TR} intersecting at E . $ST = 3x + 30$, $SR = 8x - 5$, $m\angle RTA = 5y - 2$, and $m\angle TAS = 9y + 8$

(a) Find x :



(b) Find y :