

Name: Key

Date: _____

UNIT 6

LESSON 8

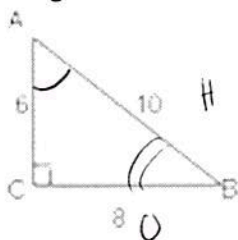
90°

AIM: WHAT ARE COFUNCTIONS?

Do Now: If two **complementary** angles are represented by $4x$ and $7x - 9$, what is the value of x ?

$$\begin{aligned} 4x + 7x - 9 &= 90 \\ 11x - 9 &= 90 \\ +9 \quad +9 & \\ \hline 11x &= 99 \\ \boxed{x=9} & \end{aligned}$$

Determine the following:



$$\sin A = \frac{8}{10} = \frac{4}{5}$$

$$\cos B = \frac{8}{10} = \frac{4}{5}$$

What is the *measure* of angle A? 53.1301

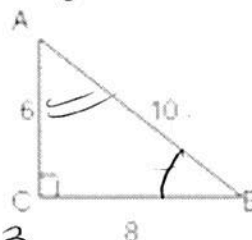
What is the *measure* of angle B? 36.8699

What is the relationship between these angles?

$$53.1301 + 36.8699 = 90^\circ$$

They are complementary!

Determine the following:



$$\sin B = \frac{6}{10} = \frac{3}{5}$$

$$\cos A = \frac{6}{10} = \frac{3}{5}$$

What is the *measure* of angle A? 36.8699

What is the *measure* of angle B? 53.1301

What is the relationship between these angles?

$$36.8699 + 53.1301 = 90^\circ$$

They are complementary!

SINE AND COSINE OF COMPLEMENTARY ANGLES

If A and B are complementary angles,

$$\begin{aligned} \sin A &= \cos B \\ \cos A &= \sin B \end{aligned}$$

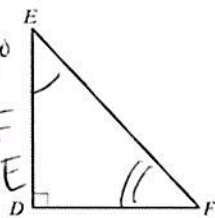
When $0^\circ < \theta < 90^\circ$, $\sin(90^\circ - \theta) = \cos \theta$ and $\sin \theta = \cos(90^\circ - \theta)$

Therefore, sine and cosine are called COFUNCTIONS!

1. In right triangle DEF, where $m\angle D = 90^\circ$, which of the following statements is always true?

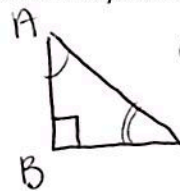
- ~~1) $\sin D = \cos F$~~
- ~~2) $\tan E = \cos F$~~
- 3) $\sin F = \cos E$
- ~~4) $\tan D = \sin E$~~

$E + F = 90^\circ$
 $\sin E = \cos F$
 $\sin F = \cos E$



2. In right triangle ABC, where $m\angle B = 90^\circ$, which of the following statements is always true?

- ~~1) $\sin A = \cos B$~~
- 2) $\sin A = \cos C$
- ~~3) $\tan A = \cos C$~~
- ~~4) $\sin A = \tan B$~~



$A + C = 90$
 $\sin A = \cos C$
 $\cos \sin C = \cos A$

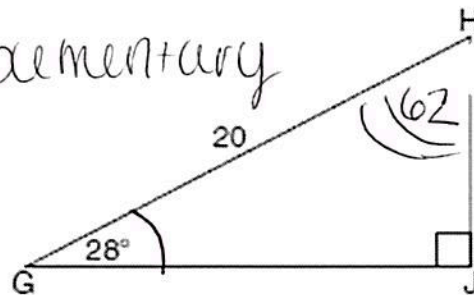
3. Each of the following diagrams and examples is a right triangle. Fill in the blanks based on the sine & cosine of angles that add to 90°

	Right Triangle ABC with $m\angle C = 90^\circ$. 	Right Triangle DEF with $m\angle E = 90^\circ$. 	
$\sin X = \cos Z$ or $\sin Z = \cos X$	$\sin A = \cos B$ or $\sin B = \cos A$	$\sin D = \cos F$ or $\sin F = \cos D$	$\sin J = \cos L$ or $\sin L = \cos J$

4. When instructed to find the length of \overline{HJ} in right triangle HJG , Jia wrote the equation $\sin 62^\circ = \frac{GJ}{20}$ while Dan

wrote $\cos 28^\circ = \frac{GJ}{20}$. Are both students' equations correct? Explain why.

yes! ($62 + 28 = 90$) G and H are complementary
 so $\sin H = \cos G$.



Sine & Cosine of Angles that add to 90°

$\sin A = \cos B$ if $A + B = 90^\circ$

5. Solve the following.

a) $\sin 27^\circ = \cos 63^\circ$
 $90 - 27 = 63$

b) $\cos 55^\circ = \sin 35^\circ$
 $90 - 55 = 35$

c) $\sin 17.8^\circ = \cos 72.2^\circ$
 $90 - 17.8 = 72.2$

d) $\cos 90^\circ = \sin 0^\circ$
 $90 - 90 = 0$

e) $\cos 45^\circ = \sin 45^\circ$
 $90 - 45 = 45$

f) $\sin 62\frac{2}{3}^\circ = \cos 27\frac{1}{3}^\circ$
 $90 - 62\frac{2}{3} = 27\frac{1}{3}$

6. Find the value of θ that will make the equation $\sin \theta = \cos 37^\circ$ true when $0^\circ < \theta < 90^\circ$. Explain your answer.

$\theta = 90 - 37 = 53^\circ$ b/c sin and cos are cofunctions
 so $\sin A = \cos B$ when A & B are complementary

set = to 90° *DO NOT SET = TO EACH OTHER!

7. In a right triangle, $\sin(2x-15)^\circ = \cos(x-12)^\circ$. What is the value of x ?

$$\underline{2x-15} + \underline{x-12} = 90$$

$$3x - 27 = 90$$

$$3x = 117$$

$$\boxed{x = 39}$$

8. In a right triangle, $\sin(x+5)^\circ = \cos(4x+10)^\circ$. What is the value of x ?

$$\underline{x+5} + \underline{4x+10} = 90$$

$$\underline{5x+15} = 90$$

$$\underline{-15} \quad \underline{-15}$$

$$5x = 75$$

$$\boxed{x = 15}$$

9. Find the value of B that will make the equation $\sin 62^\circ = \cos B$ true when $0^\circ < B < 90^\circ$. Explain your answer.

$90 - 62 = 28^\circ = B$ b/c \sin & \cos are cofunctions
so $\sin A = \cos B$ when A & B are complementary

NOW YOU TRY SOME! For questions 1-6, find values for θ that make each statement true:

1. $\sin \theta = \cos 25^\circ$

$$90 - 25 = \boxed{65}$$

2. $\sin 80^\circ = \cos \theta$

$$90 - 80 = \boxed{10^\circ}$$

3. $\sin \theta = \cos(\theta + 10)^\circ$

$$\theta + \theta + 10 = 90$$

$$2\theta + 10 = 90$$

$$\underline{2\theta = 80}$$

$$\underline{2} \quad \underline{2}$$

$$\boxed{\theta = 40}$$

4. $\sin(\theta - 45)^\circ = \cos \theta$

$$\theta - 45 + \theta = 90$$

$$2\theta - 45 = 90$$

$$2\theta = 135$$

$$\boxed{\theta = 67.5}$$

Name: Kelly

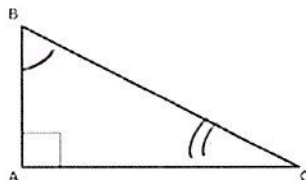
Date: _____

UNIT 6

LESSON 8

HOMEWORK

1. In scalene triangle ABC shown in the diagram below, $m\angle A = 90^\circ$. Which equation is always true?



- ~~1) $\cos C = \cos B$~~
- 2) $\sin C = \sin B$
- 3) $\sin B = \cos C$
- ~~4) $\cos B = \sin A$~~

2. In a right triangle, $\sin(5x + 15)^\circ = \cos(4x - 6)^\circ$. What is the value of x ?

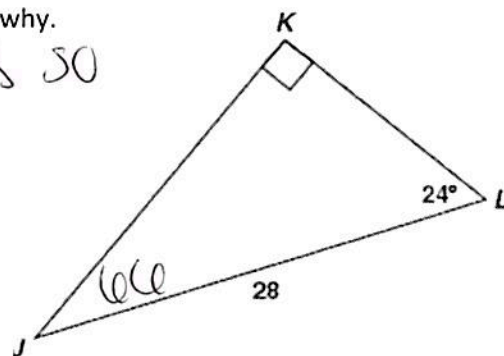
$$\begin{aligned} 5x + 15 + 4x - 6 &= 90 \\ 9x + 9 &= 90 \\ 9x &= 81 \\ \boxed{x = 9} \end{aligned}$$

4. Find the value of B that will make the equation $\sin 89^\circ = \cos B$ true when $0^\circ < B < 90^\circ$. Explain your answer.

$90 - 89 = 1 = B$
 \sin & \cos are cofunctions so $\sin A = \cos B$
 when A & B are complementary

3. When instructed to find the length of \overline{KL} in right triangle HJK , Conor wrote the equation $\cos 24^\circ = \frac{KL}{28}$ while

Steve wrote $\sin 66^\circ = \frac{KL}{28}$. Are both students' equations correct? Explain why.



Yes \sin & \cos are cofunctions so
 $\sin A = \cos B$ when $J + L$ are
 complementary

Review Question

5. As modeled below, a movie is projected onto a large outdoor screen. The bottom of the 37-foot-tall screen is 11 feet off the ground. The projector sits on the ground at a horizontal distance of 43 feet from the screen. Determine and state, to the nearest tenth of a degree, the measure of θ , the projection angle.

(Hint: Find the big angle of elevation, small angle of elevation and subtract!)

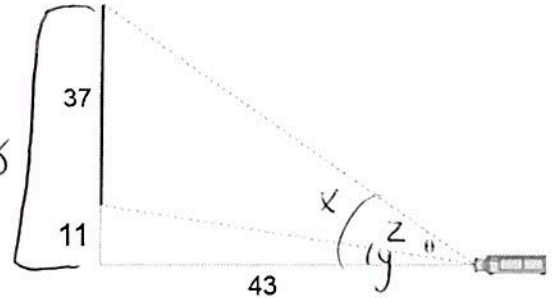
$$\star \text{Big } \Delta \star (\tan x) = \left(\frac{48}{43}\right) \tan^{-1}$$

$$x = 48.14495746$$

$$\star \text{small } \Delta \star \tan y = \frac{11}{43}$$

$$y = 14.34933204$$

$$\star \text{Subtract: } 48.14495746 - 14.34933204 = \boxed{33.8^\circ}$$



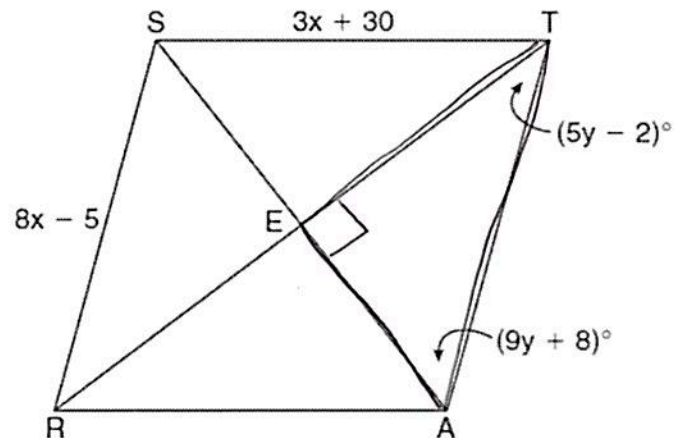
6. In the diagram below, quadrilateral $STAR$ is a rhombus with diagonals \overline{SA} and \overline{TR} intersecting at E . $ST = 3x + 30$, $SR = 8x - 5$, $m\angle RTA = 5y - 2$, and $m\angle TAS = 9y + 8$

(a) Find x :

$$\begin{array}{r} 8x - 5 = 3x + 30 \\ -3x + 5 \quad -3x + 5 \\ \hline 5x = 35 \end{array}$$

$$5x = 35$$

$$\boxed{x = 7}$$



(b) Find y :

$$\underline{5y - 2} + \underline{9y + 8} = 90$$

$$\begin{array}{r} 14y + 6 = 90 \\ -6 \quad -6 \\ \hline 14y = 84 \end{array}$$

$$14y = 84$$

$$\boxed{y = 6}$$

