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## UNIT 4

LESSON 3

## AIM: WHAT ARE THE PROPERTIES OF RHOMBUS AND SQUARES?

Do Now: The diagram below shows parallelogram $\angle M N O$ with diagonal $\overline{L N}, \mathrm{~m} \angle M=118^{\circ}$, and $\mathrm{m} \angle L N O=22^{\circ}$.
Explain why $\mathrm{m} \angle N L O$ is 40 degrees.

RHOMBUS

Judging by the markings on the picture and what you know about the properties of parallelograms and rhombi, state whether each shape is a parallelogram or a rhombus.
1.

2.

3.

4.

5.



1. In the diagram below, PQRS is a rhombus with diagonals $\overline{P R}$ and $\overline{S Q}$. If $P Q=3 x+8$ and $Q R=2 x+17$, find the value of $x$.

2. The diagonals of a rhombus have lengths of 12 centimeters and 16 centimeters. Find its perimeter.
3. In the diagram below, PQRS is a rhombus with diagonals $\overline{\mathrm{PR}}$ and $\overline{\mathrm{SQ}}$. If $\angle \mathrm{SPQ}=8 \mathrm{x}-14$ and $\mathrm{m} \angle 1=3 \mathrm{x}+3$, then find $\angle \mathrm{SPQ}$.

4. What is the length of the diagonal of a square whose side length is 12 ?
5. What is the perimeter of a square whose diagonal is $3 \sqrt{2}$ ?
6. In rhombus $A B C D$, with diagonals $A C$ and $D B$, $A D=10$. If the length of diagonal $\overline{A C}$ is 12 , what is the length of $\overline{D B}$ ?

7. In the diagram below of rhombus $A B C D$, the diagonals $\overline{A C}$ and $\overline{B D}$ intersect at $E$. If $A C=18$ and $B D=24$, what is the length of one side of rhombus $A B C D$ ?

8. In the diagram below of rhombus $A B C D, \mathrm{~m} \angle C=100$. What is $\mathrm{m} \angle D B C$ ?

9. Which set of statements would describe a parallelogram that can always be classified as a rhombus?
I. Diagonals are perpendicular bisectors of each other.
II. Diagonals bisect the angles from which they are drawn.
III. Diagonals form four congruent isosceles right triangles.
10. In parallelogram $A B C D$, diagonals $A C$ and $B D$ intersect at $E$. Which statement does not prove parallelogram $A B C D$ is a rhombus?
1) $\overline{A C} \cong \overline{D B}$
2) $\overline{A B} \cong \overline{B C}$
3) $\overline{A C} \perp \overline{D B}$
4) $\overline{A C}$ bisects $\angle D C B$
10. If $A B C D$ is a parallelogram, which statement would prove that $A B C D$ is a rhombus?
1) $\angle A B C \cong \angle C D A$
2) $\overline{A C} \cong \overline{B D}$
3) $\overline{A C} \perp \overline{B D}$
4) $\overline{A B} \perp \overline{C D}$
12. A quadrilateral whose diagonals bisect each other and are perpendicular is a
1) rhombus
2) rectangle
3) trapezoid
4) parallelogram
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## HOMEWORK

1. In the diagram below, $A B C D$ is a parallelogram, $\overline{A B}$ is extended through $B$ to $E$, and $\overline{C E}$ is drawn.


If $\overline{C E} \cong \overline{B E}$ and $\mathrm{m} \angle D=112^{\circ}$, what is $\mathrm{m} \angle E$ ?
a) $112^{\circ}$
b) $68^{\circ}$
c) $136^{\circ}$
d) $44^{\circ}$
3. Melissa is walking around the outside of a building that is in the shape of a regular polygon. She determines that the measure of one exterior angle of the building is $60^{\circ}$. How many sides does the building have?

1) 6
2) 9
3) 3
4) 12
4. 
5. In the diagram below, DEFG is a square with diagonals $\overline{\mathrm{GE}}$ and $\overline{\mathrm{DF}}$.
a) If $D E=5 x-14$ and $E F=3 x-6$, find the value of $x$.
b) If $D F=2 x-17$ and $G E=28-3 x$, find the value of $x$.

c) What is the measure of angle 4?
6. What is the perimeter of a rhombus whose diagonals are 16 and 30 ? (Hint: See Question 3 in notes!)
