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AIM: APPLYING PROPERTIES OF PARALLELOGRAMS AND RECTANGLES
Do Now: $x^{2}+5 x+6=0$

| PARALLELOGRAMS | RECTANGLES |
| :---: | :---: |
| - Opposite sides are PARALLEL. <br> - Opposite sides are CONGRUENT. <br> - Opposite angles are CONGRUENT. <br> - Consecutive angles are SUPPLEMENTARY. <br> - Diagonals BISECT each other. | ALL PROPERTIES OF PARALLELOGRAMS PLUS: <br> - Diagonals are CONGRUENT. <br> - Angles are CONGRUENT (90 degree angles) |

1. Which statement is not always true about a parallelogram?
1) The diagonals are congruent.
2) The opposite sides are congruent.
3) The opposite angles are congruent.
4) The opposite sides are parallel.
2. Which statement is true about every parallelogram?
1) All four sides are congruent.
2) The interior angles are all congruent.
3) Two pairs of opposite sides are congruent.
4) The diagonals are perpendicular to each other.
3. In the accompanying diagram of parallelogram $A B C D, \mathrm{~m} \angle A=(2 x+10)$ and $\mathrm{m} \angle B=3 x$. Find the number of degrees in $\mathrm{m} \angle B$.

4. In the accompanying diagram of parallelogram $A B C D$, diagonals $\overline{A C}$ and $\overline{B D}$ intersect at $E, B E=\frac{2}{3} x$, and $E D=x-10$. What is the value of $x$ ?

5. In the diagram below of parallelogram $A B C D$ with diagonals $\overline{A C}$ and $\overline{B D}, \mathrm{~m} \angle 1=45$ and $\mathrm{m} \angle D C B=120$. What is the measure of $\angle 2$ ?

6. As shown in the diagram below, the diagonals of parallelogram $Q R S T$ intersect at $E$. If $Q E=x^{2}+6 x$, $S E=x+14$, and $T E=6 x-1$, determine $T E$ algebraically

7. A builder is building a rectangular deck with dimensions of 16 feet by 30 feet. To ensure that the sides form $90^{\circ}$ angles, what should each diagonal measure?
8. As shown in the diagram of rectangle $A B C D$ below, diagonals $\overline{A C}$ and $\overline{B D}$ intersect at $E$. If $A E=x+2$ and $B D=4 x-16$, then the length of $\overline{A C}$ is

9. As shown in the accompanying diagram, a rectangular gate has two diagonal supports. If $m \angle 1=42$, what is $m \angle 2$ ?

10. In the accompanying diagram of rectangle $A B C D, \mathrm{~m} \angle B A C=3 x+4$ and $\mathrm{m} \angle A C D=x+28$. What is $\mathrm{m} \angle C A D$ ?

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## EXTRA PRACTICE

1. A parallelogram is always a rectangle if
1) the diagonals are congruent
2) the diagonals bisect each other
3) the diagonals intersect at right angles
4) the opposite angles are congruent
2. In the diagram below, $A B C D$ is a parallelogram, $A B$ is extended through $B$ to $E$, and $\overline{C E}$ is drawn.


If $\overline{C E} \cong \overline{B E}$ and $\mathrm{m} \angle D=112^{\circ}$, what is $\mathrm{m} \angle E$ ?

In parallelogram $R S T U, \mathrm{~m} \angle R=5 x-2$ and $\mathrm{m} \angle S=3 x+10$. Determine and state the value of $x$.
5. In the accompanying diagram of parallelogram $A B C D$, diagonals $\overline{A C}$ and $\overline{D B}$ intersect at $E$, $A E=3 x-4$, and $E C=x+12$.


What is the value of $x$ ?

In the diagram below of rectangle $R S T U$, diagonals $\overline{R T}$ and $\overline{S U}$ intersect at $O$.


If $R T=6 x+4$ and $S O=7 x-6$, what is the length of $\overline{U S}$ ?

