

Name: Key

Date: \_\_\_\_\_

UNIT 3

REVIEW

REVIEW #1: CUT-OUT PROOFS

Directions: Match the statements and reasons for each proof. Write the full proof in this packet.

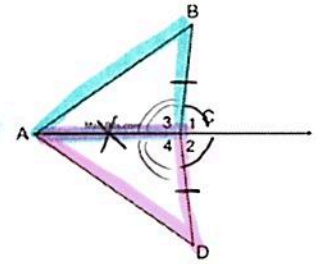
EXAMPLE #1: PINK

Given:  $\overline{BC} \cong \overline{CD}$   
 $\angle 1 \cong \angle 2$

S ✓  
A ✓  
S ✓

Prove:  $\triangle BAC \cong \triangle DAC \rightarrow$  CPCTC

1st  $\triangle BAC \cong \triangle DAC$   
STATEMENT



REASON

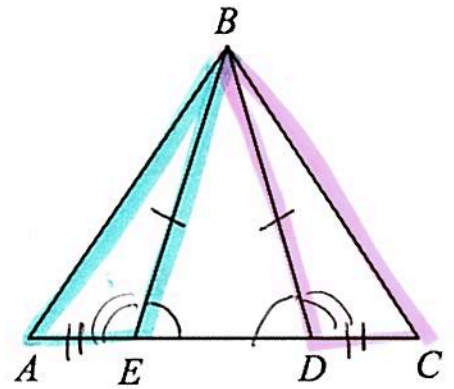
① $\overline{BC} \cong \overline{CD}$ ✓ (S) $\angle 1 \cong \angle 2$	① Given
② $\angle 1 + \angle 3 = 180^\circ$ $\angle 2 + \angle 4 = 180^\circ$	② Linear pairs are supplementary
③ $\angle 3 \cong \angle 4$ ✓ (A)	③ supplements of $\cong$ $\angle$ 's are $\cong$
④ $\overline{AC} \cong \overline{AC}$ ✓ (S)	④ Reflexive Property
⑤ $\triangle BAC \cong \triangle DAC$	⑤ SAS $\cong$ SAS
⑥ $\angle BAC \cong \angle DAC$	⑥ CPCTC

**EXAMPLE #2: BLUE**

Given:  $\overline{BE} \cong \overline{BD}$  &  $\overline{AE} \cong \overline{CD}$

Prove:  $\triangle ABC$  is isosceles

- ③  
 ② need:  $\angle A \cong \angle C$  by CPCTC SV  
\*A ✓  
S  
 ① need:  $\triangle ABE \cong \triangle CBD$



STATEMENT	REASON
① $\overline{BE} \cong \overline{BD}$ , $\overline{AE} \cong \overline{CD}$ ✓ (S)	① Given
② $\triangle BED$ is isosceles	② Isosceles $\triangle$ 's have 2 $\cong$ sides
③ $\angle BED \cong \angle BDE$	③ Isosceles $\triangle$ 's have 2 $\cong$ base $\angle$ 's
④ $\angle BED + \angle BEA = 180^\circ$ $\angle BDE + \angle BDC = 180^\circ$	④ Linear pairs are supplementary
⑤ $\angle BEA \cong \angle BDC$ ✓ (A)	⑤ Supplements of $\cong$ $\angle$ 's are $\cong$
⑥ $\triangle ABE \cong \triangle CBD$	⑥ SAS $\cong$ SAS
⑦ $\angle A \cong \angle C$	⑦ CPCTC
⑧ $\triangle ABC$ is isosceles	⑧ Isosceles $\triangle$ 's have 2 $\cong$ base $\angle$ 's

**EXAMPLE #3: GREEN**

Given:  $\overline{CB} \perp \overline{DA}$

(3)  $\overline{DC} \cong \overline{AC}$

Prove: B is the midpoint of  $\overline{DA}$

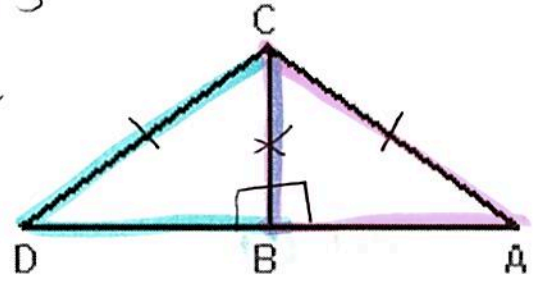
(2)  $\hookrightarrow \overline{DB} \cong \overline{BA}$  by CPCTC

(1)  $\hookrightarrow \triangle CBD \cong \triangle CBA$  by HL

Right  $\Delta$ 's  $\checkmark$

H  $\checkmark$

L  $\checkmark$



STATEMENT

REASON

(1)  $\overline{CB} \perp \overline{DA}$ ,  $\overline{DC} \cong \overline{AC}$   $\checkmark$  (H)

(1) Given

(2)  $\overline{CB} \cong \overline{CB}$   $\checkmark$  (L)

(2) Reflexive property

(3)  $\angle CBD$  and  $\angle CBA$  are right  $\angle$ 's

(3)  $\perp$  lines form right  $\angle$ 's

(4)  $\triangle CBD$  and  $\triangle CBA$  are right  $\Delta$ 's  $\checkmark$  (right  $\Delta$ 's)

(4) Right  $\Delta$ 's have 1 right  $\angle$

(5)  $\triangle CBD \cong \triangle CBA$

(5) HL  $\cong$  HL

(6)  $\overline{DB} \cong \overline{BA}$

(6) CPCTC

(7) B is the midpoint of  $\overline{DA}$

(7) A midpoint creates 2  $\cong$  segments

**EXAMPLE #4: YELLOW**

\* ISOSCELES  $\Delta$ 's \*

Given:  $\Delta H \cong \Delta J$

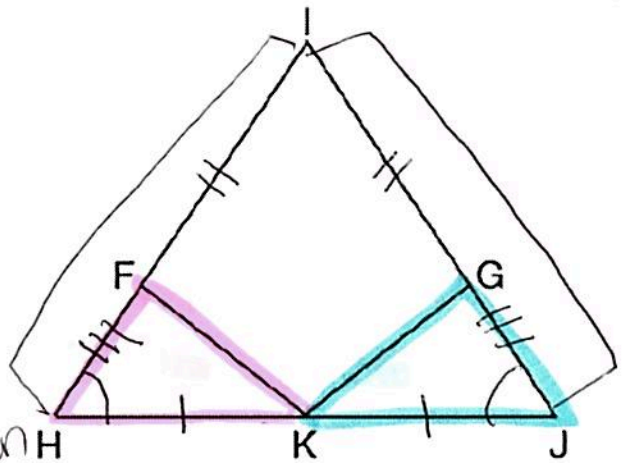
K is the midpoint of  $\overline{HJ}$

$\overline{IF} \cong \overline{IG}$

Prove:  $\overline{FK} \cong \overline{GK} \rightarrow$  CPCTC

$\hookrightarrow \Delta FHK \cong \Delta GJK$

S  $\checkmark$   
 A  $\checkmark$   
 \* S  $\checkmark$   
 ↓  
 SUBTRACTION  
 PROPERTY



STATEMENT

REASON

①  $\Delta H \cong \Delta J \checkmark$  (A)  
 K is the midpoint of  $\overline{HJ}$   
 $\overline{IF} \cong \overline{IG}$

① given

②  $\overline{HK} \cong \overline{KJ} \checkmark$  (S)

② A midpoint creates 2  $\cong$  segments

③  $\Delta HIJ$  is isosceles

③ isosceles  $\Delta$ 's have 2  $\cong$  base  $\Delta$ 's

④  $\overline{IH} \cong \overline{IJ}$

④ isosceles  $\Delta$ 's have 2  $\cong$  sides

⑤  $\overline{FH} \cong \overline{GJ} \checkmark$  (S)

⑤ subtraction property

$FH = IH - IF$

$GJ = IJ - IG$

⑥  $\Delta FHK \cong \Delta GJK$

⑥ SAS  $\cong$  SAS

⑦  $\overline{FK} \cong \overline{GK}$

⑦ CPCTC

**EXAMPLE #5: GRAY**

Given:  $\overline{AE} \cong \overline{DF}$

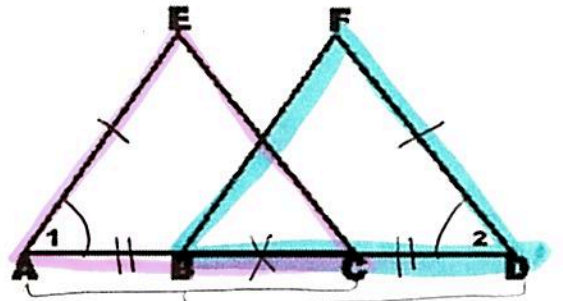
$\angle 1 \cong \angle 2$

$\overline{AB} \cong \overline{CD}$

Prove:  $\triangle AEC \cong \triangle BFD$

S ✓  
A ✓  
\*S ✓  
↓

addition property



STATEMENT

REASON

①  $\overline{AE} \cong \overline{DF}$ ,  $\angle 1 \cong \angle 2$  ✓ (S)  
 $\overline{AB} \cong \overline{CD}$

① Given

②  $\overline{BC} \cong \overline{BC}$

② Reflexive Property

③  $\overline{AC} \cong \overline{BD}$  ✓ (S)  
 $\overline{AC} = \overline{AB} + \overline{BC}$   
 $\overline{BD} = \overline{DC} + \overline{BC}$

③ Addition Property

④  $\triangle AEC \cong \triangle BFD$

④ SAS  $\cong$  SAS

